Math

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### Endorsements



### **Sponsorships**







### Summary of Activities:

Setting the Stage Carousel Activity Summarizing the Results Understanding Scale Understanding Bacterial Growth Bacterial Growth Demonstration Application of Knowledge Is it Safe to Eat? Student Reflection Analyzing Bacterial Growth Data Analyzing Data Self-Assessment

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| Day    |        | Math Common Core Standards  |
|--------|--------|---|
| Day 1  | 8.SP.4 | Understand that patterns of association can also be seen in bivariate categorical data by displaying frequencies and relative frequencies in a two-way table. Construct and interpret a two-way table summarizing data on two categorical variables collected form the same subjects. Use relative frequencies calculated for rows or columns to describe possible association between the two variables. |
|        |        |   |
| Day 2  | 8.G.4  | Understand that a two-dimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and <b>dilations</b> .   |
| Day 2  | 8.G.9  | Know the formulas for the volumes of cones, <b>cylinders</b> , and spheres and use them to solve real-world and mathematical problems   |
|        |        |   |
|        | 8.F.1  | Understand that a function is a rule that signs to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output.  |
| Day 3  | 8.F.3  | Give examples of functions that are not linear.   |
|        | 8.F.5  | Describe qualitatively the functional relationship between two quantities by analyzing a graph (e.g. where the function is increasing or decreasing, linear or nonlinear).  |
|        |        |   |
| Day 4  | 8.F.1  | Understand that a function is a rule that signs to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output.  |
|        | 8.F.3  | Give examples of functions that are not linear.   |
|        |        |   |
| Dave 5 | 8.SP.1 | Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative association, linear association, and nonlinear association.  |
| Days 5 | 8.SP.2 | Know that straight lines are widely used to model relationships between two quantitative variables. For scatter plots that suggest a linear association, informally fit a straight line, and informally assess the mode fit by judging the closeness of the data points to the line.  |

Robert Gagne's Nine Events of Effective Instruction-Math

| Stage of         | Event                                      | Description  | Math Activity                      |
|------------------|--|--|------------------------------------|
| Instruction      |  |  |                                    |
| tion             | Gaining<br>Attention                       | Stimulates readiness to learn and<br>participate. Stimuli like surprises or<br>questions are typically used for this<br>event.   | Setting the Stage                  |
| Pre-Instruction  | Informing<br>learners of the<br>objectives | Generates expectancy by helping<br>them understand what they will be<br>learning   | Inform learners of the objectives  |
| Pr               | Stimulating recall of prior                | Relating new information to something they already know or have  | Carousel Activity                  |
|                  | learning                                   | experienced helps learners make<br>sense of the lesson   | Graphing Data                      |
|                  | Presenting the                             | New information is presented.<br>Strategies like providing examples or   | Understanding Scale                |
| ion              | stimulus                                   | presenting vocabulary should be used<br>to present the lesson content to<br>provide more effective instruction   | Understanding<br>Bacterial Growth  |
| Instruction      | Providing<br>learning<br>guidance          | Helps facilitate the process of long-<br>term information storage  | Bacterial Growth<br>Demonstration  |
|                  | Eliciting<br>performance                   | Requires the learner to practice the<br>new skill or behavior. The repetition<br>further increases the likelihood of<br>retention of the new information   | Application of<br>Knowledge        |
|                  | Providing<br>feedback                      | Assess and further facilitate learning.<br>Typically, activities designed for<br>feedback are for comprehension, not<br>scoring  | Is it Safe to Eat?                 |
| Post-Instruction | Assessing performance                      | To evaluate the effectiveness of the<br>instructional events, you must test to<br>see if the expected learning outcomes<br>have been achieved  | Student Reflection                 |
| Post-I           | Enhancing<br>retention and<br>transfer     | Helps learners develop expertise by<br>internalizing the new information.<br>Methods for helping learners<br>internalize are paraphrasing,<br>generating examples, creating<br>concept maps or outlines, and<br>repetition | Analyzing Bacterial<br>Growth Data |

| Unit Activities:<br>Materials:<br>Student<br>Handouts: | Setting the Stage, Objectives,<br>Carousel Survey<br>Carousel prompts (pgs. M6-M17),<br>calculators (optional), construction<br>paper, and markers<br><i>Summarizing the Results</i> (pg.18-19) | Learning<br>Objectives:<br>Common Core<br>Standards: | <ul> <li>Students will be able to: <ol> <li>Develop and organize a data set generated from class responses.</li> <li>Use equivalent forms of proportions, ratios, and percent to describe, summarize, and interpret survey results.</li> <li>Use information to present data and findings.</li> </ol> </li> <li>8.SP.4</li> </ul> |
|--|---|--|---|
| Activities:  |   |  |   |
| Setting the  | Purpose: To capture attention and pre   | pare students to le                                  | earn and participate.   |
| Stage<br>(8 minutes)                                   | Learner Level: All  |  |   |
|  | • Write the following question on the board or overhead: <b>Describe what we mean when</b>  |  |   |
|  | we say a human grows.   |  |   |
|  | <ul> <li>Ask students to write down their response to the question. Allow 3-5 minutes for</li> </ul>  |  |   |
|  | students to do so.  |  |   |
|  | <ul> <li>Allow students to share their responses with the class.</li> </ul>   |  |   |
|  | <ul> <li>Pose questions for disc</li> </ul>   | cussion:   |   |
|  | <ul> <li>How much hav</li> </ul>  |  | -   |
|  | <ul> <li>As we know, humans are a type of animal. What has to happen</li> </ul>   |  |   |
|  | biologically to make an animal, such as a human, grow? (cell division)  |  |   |
|  | <ul> <li>Is this process also required for other types of organisms such as plants<br/>or bacteria to grow?</li> </ul>  |  |   |
|  | or bacteria to g  | 310W (   |   |
| Inform the   | Purpose: To help students understand  | what they are resp                                   | ponsible for learning.  |
| Learner of the<br>Objectives<br>(2 minutes)            |   | acteria. Our firs                                    | y the difference in the growth of<br>t activity is going to investigate how<br>nome.  |
|  |   |  |   |

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| Carousel<br>Activity<br>(30 minutes)       | Purpose: To familiarize students with new words, activate prior knowledge, and provide a guide to the concepts they will learn in this lesson.  |
|--|---|
|  | <ul> <li>Before beginning this activity, copy each question from the Carousel Activity (pgs. M8-M17).</li> <li>Post each page in a different place around the room.</li> <li>Divide students into 10 groups and send each group to a different page.</li> <li>Give students 1-2 minutes to read the question on their page and then tally their response in the appropriate box in the answer grid.</li> <li>Rotate student groups to a new page every 2-3 minutes until each group has answered every question.</li> <li>Discuss each question with the class, noting the various answers. Discuss the best answer choice(s) for each question.</li> </ul>   |
| Summarizing<br>the Results<br>(20 minutes) | <ul> <li>Learner Level: All <ul> <li>Assign each group of students one of the question pages from the Carousel Activity above.</li> <li>Each group should convert the data (student responses tallied) from their assigned questions to a number representing the frequency of students who selected each response per question.</li> <li>Post the frequency for each response per item on the board and instruct students to use this data to complete the Summarizing the Results handout. You may need to review finding percent, ratio, and fractions with students.</li> <li>On this handout, students will practice representing the responses given as equivalent forms of fractions, percentages, and ratios, and then write 3 sentences describing results.</li> <li>Walk through the example problem on the Summarizing the Results handout with students.</li> <li>After students finish, have them share some of their sentences with a partner or with the class, have students or partners create a graph (pie, bar, line, etc) to display their results in a creative way. They also need to include an advertising statement based on the current answers to the food safety facts they learned.</li> </ul> </li> </ul> |
| Wrap Up<br>(5 minutes)                     | Tell students: <b>Today we collected, analyzed, and summarized data about our food safety</b><br>practices. Then, we used the information to create targeted food safety messages.<br>Tomorrow we will learn about scale and get a better grasp of how small bacteria are.  |

- 1. I clean the area where I make food and snacks before and after making food and snacks.
  - a. Never
  - b. Sometimes
  - c. Usually
  - d. Always

| Α | В |
|---|---|
| C | D |

- 2. The last time there was cookie dough in my home, the dough was:
  - a. Made with raw eggs, and I sampled some of it
  - b. Made with raw eggs and refrigerated, then I sampled some of it
  - c. Store-bought, and I sampled some of it
  - d. Not sampled until baked

| A | В |
|---|---|
| С | D |

- 3. Meat, poultry, and fish products are defrosted in my home by:
  - a. Setting them on the counter
  - b. Placing them in the refrigerator
  - c. Microwaving
  - d. I don't know

| Α | B |
|---|---|
| С | D |

- 4. I know the types of foods that put me at a higher risk for getting food poisoning.
  - a. Strongly disagree
  - b. Disagree
  - c. Agree
  - d. Strongly agree

| Α | В |  |
|---|---|--|
| С | D |  |
|   |   |  |

- 5. When cooking meat I use a thermometer to check the temperature and doneness of the meat.
  - a. Never
  - b. Sometimes
  - c. Usually
  - d. Always

| Α | В |
|---|---|
| C | D |
|   |   |

- 6. The temperature of the refrigerator in my home is:
  - a. 50 degrees Fahrenheit
  - b. 40 degrees Fahrenheit
  - c. 20 degrees Fahrenheit
  - d. I don't know; I've never measured it

| A | В |  |
|---|---|--|
| С | D |  |
|   |   |  |

- I can positively impact the safety of my food by keeping cooked foods at room temperature for longer than 2 hours.
  - a. Strongly disagree
  - b. Disagree
  - c. Agree
  - d. Strongly agree

| Α | В |
|---|---|
| C | D |

- 8. I feel that it is an adult's responsibility to keep my food safe when handling food.
  - a. Strongly disagree
  - b. Disagree
  - c. Agree
  - d. Strongly agree

| Α | В |
|---|---|
| C | D |
|   |   |

- 9. If a cutting board is used in my home to cut raw foods and it is going to be used to chop another food, the board is:
  - a. Reused as is
  - b. Wiped with a damp cloth
  - c. Washed with soap and hot water
  - d. Washed with soap and hot water and then sanitized

| Α | В |
|---|---|
| С | D |

- 10. I wash my hands before and after preparing snacks and meals
  - a. Never
  - b. Rarely
  - c. Sometimes
  - d. Always

| Α | В |
|---|---|
| C | D |
|   |   |

### **Carousel Heading Explanations**

### 1. I clean the area where I make food and snacks before and after making food and snacks.

- a. Never
- b. Sometimes
- c. Usually
- d. Always
  - The kitchen is one of the most dangerous places in the house because of the infectious bacteria that are sometimes found in raw foods.
  - Germs are easily spread to other people in the kitchen because food is prepared here.
  - Dirt and germs live on tables, countertops, and other places in the kitchen where food is prepared.

#### 2. The last time there was cookie dough in my home, the dough was:

- a. Make with raw eggs, and I sampled some of it
- b. Make with raw eggs and refrigerated, then I sampled some of it
- c. Store-bought, and I sampled some of it
- d. Not sampled until I ate the baked cookies
  - Eating raw cookie dough may put you at risk for infection with *Salmonella enteritidis*, a bacterium that can be inside eggshells.
  - Refrigerating will <u>not</u> kill the bacteria.
  - Other foods containing raw eggs, such as homemade ice cream, cake batter, mayonnaise, and eggnog, carry a *Salmonella* risk, too.
  - Their commercial counterparts are usually made with pasteurized eggs; that is, eggs that have been heated sufficiently to kill bacteria. However, there is still a risk to consuming the commercial cookie dough products without baking them.

### 3. Meat, poultry, and fish products are defrosted in my home by:

- a. Setting them on the counter
- b. Placing them in the refrigerator
- c. Microwaving
- d. I don't know
  - Gradual defrosting overnight in the refrigerator is best because it helps maintain quality
  - Using the microwave oven or putting the packaging in a water-tight plastic bag submerged in cold water and changing the water every 30 minutes are also safe ways to defrost.
  - Do <u>not</u> thaw meat, poultry, and fish products on the counter or in the sink without cold water; bacteria can multiply rapidly at room temperature.
  - Marinate food in the refrigerator, not on the counter. Discard the marinade after use because it contains raw juices, which may harbor bacteria.

### 4. I know the types of foods that put me at a higher risk for getting food poisoning.

- a. Strongly disagree
- b. Disagree
- c. Agree
- d. Strongly agree
  - Salmonella: Raw meats, poultry, eggs, dairy products
  - *E. coli* 0157:H7: Ground beef, fruits, vegetables, raw milk
  - *Listeria*: Deli meats, hot dogs, soft cheese, imported seafood products
  - *Campylobacter jejuni*: Raw poultry, meat, and unpasteurized milk
  - *Staphylococcus aureus*: Meats, poultry, egg products, mayonnaise based products

### 5. When cooking meat I use a thermometer to check the temperature and doneness of the meat.

- a. Never
- b. Sometimes
- c. Usually
- d. Always
  - Using a digital or dial food thermometer is important.
  - Cooking by color is misleading.
  - Some ground meat may prematurely brown before a safe internal temperature has been reached.

#### 6. The temperature of the refrigerator in my home is:

a. 50 degrees Fahrenheit

b. 40 F

- c. 20 F
- d. I don't know; I've never measured it
  - Refrigerators should stay at 40°F or less because it slows the growth of most bacteria.
  - The temperature won't kill the bacteria, but it will keep them from multiplying, and the fewer there are, the less likely you are to get sick.
  - According to surveys, in many households, the refrigerator temperature is above 50 F.
  - Measure the temperature with a thermometer and, if need, adjust the refrigerator's temperature control dial.

## 7. I can positively impact the safety of my food by keeping cooked foods at room temperature for longer than 2 hours.

- a. Strongly disagree
- b. Disagree
- c. Agree
- d. Strongly agree
  - Refrigerator or freeze leftovers within 2 hours or sooner to prevent harmful bacteria from multiplying.
  - Cold temperatures keep most harmful bacteria from growing and multiplying.
  - Bacteria grow most rapidly at unsafe temperatures between 40°F 140°F.

### 8. I feel that it is an adult's responsibility to keep my food safe when handling food.

- a. Strongly disagree
- b. Disagree
- c. Agree
- d. Strongly agree
  - We have an individual responsibility for the food that we eat.
  - Taking actions such as washing hands, storing foods properly, cooking foods properly, and being aware of the foods that cause foodborne illness outbreaks will help in preventing a foodborne illness.

## 9. If a cutting board is used to cut raw foods and it is going to be used to chop another food, the board is:

- a. Reused as is
- b. Wipes with a damp cloth
- c. Washed with soap and hot water
- d. Washed with soap and hot water and then sanitized
  - Use smooth cutting boards of hard maple or plastic and free of cracks and crevices.
  - Wash cutting boards with hot water, soap, and a scrub brush to remove food particles. Then sanitize the boards by putting them through the automatic dishwasher or rinsing them in a solution of 1 teaspoon of chlorine bleach in 1 quart of water.
  - Always wash and sanitize cutting boards after using them for raw foods and before using them for ready-to-eat foods.

### 10. I wash my hands before and after preparing snacks and meals

- a. Never
- b. Rarely
- c. Sometimes
- d. Always
  - The most important thing that you can do to keep from getting sick is to wash your hands.
  - Frequently washing hands allows you to wash away germs that could have been picked up from other people, contaminated surfaces, or from animals and animal waste.



Summarizing the Results



**Directions:** Pick 2 of the questions from the Carousel Activity and report the frequency of responses given for each answer choice. Then, using the proportion of the frequency of response to the total # of responses given, create equivalent forms of the proportion (percent, fraction, ratio). Use the statistics of the data collected to summarize the results.

### EXAMPLE:

Question #: 1

Total # of Responses: 25

| CHOICE A  |                |                   |          |           | CHO            | ICE B             |       |
|-----------|----------------|-------------------|----------|-----------|----------------|-------------------|-------|
| Frequency | Percent        | Fraction          | Ratio    | Frequency | Percent        | Fraction          | Ratio |
| 2         | 8%             | 2/25              | 2:25     | 7         | 28%            | 7/25              | 7:25  |
| CHOICE C  |                |                   | CHOICE D |           |                |                   |       |
|           | CHO            | ICE C             |          |           | CHO            | ICE D             |       |
| Frequency | CHO<br>Percent | ICE C<br>Fraction | Ratio    | Frequency | CHO<br>Percent | ICE D<br>Fraction | Ratio |

Now using the data above, write 3 statements with proportions and relationships describing the results.

- 1. Four out of 5 students **Usually** or **Sometimes** (*Sum of Choices B and C converted to a ratio*) cleans the area where they make food and snacks.
- 2. Only 8% said they **Never** (*Choice A*) clean the area where they make food and snacks; whereas 92% said they cleaned the area at least some of the time (*Sum of Choices B, C, and D*).
- 3. Over half of the students, indicated that they **Usually** (*Choice C*) clean the area where they make food and snacks.

**<u>PRACTICE</u>**: As a class or in groups, create two other summary sentences for the responses provided in the example.

1.

2.

### **YOUR TURN:**

| Question # _ |                 |                  |       |           | Total          | # of Respons      | es:   |
|--------------|-----------------|------------------|-------|-----------|----------------|-------------------|-------|
| CHOICE A     |                 |                  |       |           | CHO            | ICE B             |       |
| Frequency    | Percent         | Fraction         | Ratio | Frequency | Percent        | Fraction          | Ratio |
|              |                 |                  |       |           |                |                   |       |
| CHOICE C     |                 |                  |       |           |                |                   |       |
|              | CHO             | CE C             |       |           | CHO            | ICE D             |       |
| Frequency    | CHOI<br>Percent | CE C<br>Fraction | Ratio | Frequency | CHO<br>Percent | ICE D<br>Fraction | Ratio |
| Frequency    |                 |                  | Ratio | Frequency |                |                   | Ratio |

Now using the data above, write 3 statements with proportions and relationships describing the results.

1.

- 2.
- 2.
- 3.

Question #

Total # of Responses:

| <u> </u>  |                |                   |       |           | 1000           | 1                 |       |
|-----------|----------------|-------------------|-------|-----------|----------------|-------------------|-------|
| CHOICE A  |                |                   |       | CHO       | ICE B          |                   |       |
| Frequency | Percent        | Fraction          | Ratio | Frequency | Percent        | Fraction          | Ratio |
|           |                |                   |       |           |                |                   |       |
|           |                |                   |       |           |                |                   |       |
|           | СНО            | ICF C             |       |           | СНО            | ICF D             |       |
|           | CHO            | ICE C             |       |           | CHO            | ICE D             |       |
| Frequency | CHO<br>Percent | ICE C<br>Fraction | Ratio | Frequency | CHO<br>Percent | ICE D<br>Fraction | Ratio |
| Frequency |                |                   | Ratio | Frequency |                |                   | Ratio |

Now using the data above, write 3 statements with proportions and relationships describing the results.

1.

3.

2.

<u>**Think About It:**</u> After completing this carousel activity, how do you think other students would answer the questions? Would the results be the same, similar, or different? Why or why not?

| Unit Activities:<br>Instructional<br>Events:<br>Materials: | Review, Understanding Scale<br>Present the stimulus<br>Rulers, calculators, construction<br>paper, tape, scissors, soda can(s)   | Learning<br>Objectives:   | <ol> <li>Students will be able to:         <ol> <li>Recognize and understand<br/>microscope magnification an<br/>object by 4x, 10x, and 40x as an<br/>example of scale factors and<br/>dilation.</li> <li>Apply use of scale factors and<br/>dilation to create 3-D scaled<br/>models of a cylinder.</li> <li>Calculate surface area and<br/>volume of a cylinder in scaled<br/>relationships.</li> </ol> </li> </ol> |  |
|--|--|---|---|--|
| Student<br>Handouts:                                       | <i>Understanding Scale</i> worksheet<br>with <i>Grid</i> (pg. M22), <i>Understanding</i><br><i>Scale in 3D</i> worksheet (pg. M23)   | Common Core<br>Standards:   | 8.G.4<br>8.G.9  |  |
| Activities:  |  |   |   |  |
| Review   |  | •   | o see how likely bacteria were to grow  |  |
| (5 minutes)  | in our kitchens. what changes did  | you suggest to yo   | ur parents last night during dinner?  |  |
|  | Today we will talk about scale fact  | ors and try to get  | an idea of the size of bacteria.  |  |
| Understanding<br>Scale<br>(20 minutes)                     | <ul> <li>learned in science class that bacteria</li> <li>Ask: How big is a single bacterium</li> <li>Then, explain to students that bac<br/>magnified using a microscope. La</li> </ul>  | is plural (more than<br>n? Allow students t<br>cteria are microsco<br>ter in the week stu | -   |  |
|  | <ul> <li>bacteria at 4x, 10x, and 40x its actual size.</li> <li>How is Magnification related to math? Magnification is a type of dilation. A <i>dilation</i> is a transformation that produces an image the same shape as the original, but is a different size. Like drawing a figure to scale. Or, in our case, using a microscope to magnify the image of the bacteria. The <i>scale factor</i> is a measure of the dilation, that is, how much larger or smaller the image is. The microscope has 3 lenses which allow us to view the image at scale factors of 4x, 10x, and 40x.</li> </ul> |   |   |  |
|  | HINTS: Have students draw a sma<br>dashed box to allow room for dila   | all quadrilateral wintions. For beginne   | e <b>Understanding Scale</b> worksheet.<br>ithin the first coordinates denoted by the<br>ers, you might suggest a square<br>udents, you might require a polygon with  |  |
|  |  | -   | outside and 1) using a measuring stick,<br>nes or people as endpoints, plot a shape   |  |
|  | on the football field and dilate by 4x a   |   | ווכס סד פרטטוב מס בוועףטווונס, פוטג מ סוומפי  |  |
|  |  |   |   |  |

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| <i>Activities:</i><br>Understanding<br>Scale in 3D<br>(30 minutes) | <ul> <li>Explain to students that, unlike the 2-dimensional examples in the <i>Understanding Scale</i> activity, bacteria is 3-dimensional. Dilation (scale) is proportional and occurs in all dimensions.</li> <li>To explore this concept, students will construct a 3-D model of a soda can (cylinder) at actual size (1x), and scaled to 4x and 10x.</li> <li>Using construction paper and tape, have students construct a 3-D model of a soda can (cylinder) out of 2 circles and a rectangle. This represents the actual size or 1x. Options: Let students measure a soda can or provide them with the dimensions.</li> <li>Have students create 3-D dilations of the cylinder at scale factors of 4 and 10.</li> </ul> |
|--|---|
|  | <u>Optional Supplemental Activity</u> : Allow students to calculate how big the soda can would be at 40x, and then create a huddle of students the same size. How many students would it take?  |
|  | • For each model, complete the corresponding <i>Understanding Scale in 3D</i> worksheet which extends from previous activity and examines how <u>Surface Area</u> and <u>Volume</u> change when dilated.  |
|  | Surface Area: How much aluminum would it take to make a soda can?   |
|  | What do we know: Cylinder = 2 circles + rectangle   |
|  | Area of a Circle = $\pi r^2$ and Area of Rectangle = $l \bullet w$  |
|  | In a cylinder, the <i>length</i> is the circumference of the circle, and the <i>width</i> is the height of the can.   |
|  | So: Surface Area of a Cylinder = 2(area of a circle) + (circumference • height)   |
|  | $SA = 2\pi r^2 + 2\pi r \cdot h$  |
|  | <b>Volume</b> : How much liquid could the soda can hold?  |
|  | What do we know: Volume is the area of the base multiplied by the height.   |
|  | So: Volume of a Cylinder = Area of Circle • Height of Can   |
|  | $\mathbf{V} = \mathbf{\pi} r^2 \bullet h$   |
|  | <b>Connect</b> : Explain to students that when they look at their bacteria in the microscope the 4x, 10x, and 40x are the powers of magnification they will use. Encourage students to draw connections between the actual sizes of the can versus the 40x.   |
| Wrap Up<br>(5 minutes)   | <ul> <li>Ask students one or two Critical Thinking Questions:</li> <li>What does <i>Figure Drawn to Scale</i> mean?</li> <li>What does <i>Figure is NOT Drawn to Scale</i> mean?</li> </ul>   |
|  | The difference between being drawn to scale and not drawn to scale is proportionality.  |
|  | Tomorrow we will talk about bacterial growth using charts and exponential curves.   |

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- **Step 1**: Draw a polygon within the small box marked on the grid paper. This is your original figure, with a scale factor of 1.
- Step 2: Label the vertices and write the scale factor inside the figure.
- Step 3: Fill in the properties of the original figure in the table below.
- Step 4: Dilate the figure by a scale factors of 4 and 10 to complete the table.

| For examp  | le  |   |                 |                                |
|------------|-----|---|-----------------|--------------------------------|
| i or examp | 10. |   | Properties      | <b>Original Figure</b>         |
| Α          |     | В | Scale Factor    | 1                              |
|            | 4   |   | Coordinates     | A(2,3), B(6,3), C(6,1), D(2,1) |
|            | 1   |   | Angle Measures  | A: 90°, B: 90°, C: 90°, D: 90° |
| D          |     | C | Length of Sides | AB: 4, BC:2, CD: 4, DA: 2      |
|            |     |   | Perimeter       | 12 units                       |
|            |     |   | Area            | 8 units <sup>2</sup>           |

| Properties      | Original Figure | Dilate <u>original</u> by a<br>Scale Factor of 4 | Dilate <u>original</u> by a<br>Scale Factor of 10 |
|-----------------|-----------------|--|---|
| Coordinates     |                 |  |   |
| Angle Measures  |                 |  |   |
| Length of Sides |                 |  |   |
| Perimeter       |                 |  |   |
| Area            |                 |  |   |

### **Connect and Make Generalizations**

| Properties     | <b>Observations and Conjectures</b> |
|----------------|-------------------------------------|
| Coordinates    |                                     |
| Angle Measures |                                     |
| Length         |                                     |
| Perimeter      |                                     |
| Area           |                                     |

How does the scale factor influence each of the figure's properties during dilation?

**CHALLENGE**: Using these observations, complete the answer the following questions for the dilation of your original figure by a <u>scale factor of 40</u>.

| Coordinates     |  |
|-----------------|--|
| Angle Measures  |  |
| Length of Sides |  |
| Perimeter       |  |
| Area            |  |

# Grid for Understanding Scale

|           |          |                    |          | 24       |          | ٦Ľ |          | Ľ٦       |            | U          | Ц          | Ľ. | 5        | R        | স | 50 | ЛЦ        | ľ. | μп       |          | 3        | U |          | a | 5            |          |           |   |          |
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|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
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|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          | $\square$ |   |          |
|           | -        |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          | $\square$ |   |          |
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|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
| $\square$ |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |
|           |          |                    |          |          |          |    |          |          |            |            |            |    |          |          |   |    |           |    |          |          |          |   |          |   |              |          |           |   |          |

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# Understanding Scale in 3D

**Directions:** Using the 3-D scale models of the soda can, fill in the measurements, and then find the **Surface Area** and **Volume** for each dilation.

| Surface Area: Ho |   |            |
|------------------|---|------------|
| What do we know: | Cylinder = 2 circles + rectangle  | $\bigcirc$ |
|                  | Area of a Circle = $\pi r^2$ and Area of Rectangle = $l \cdot w$  |            |
|                  | ylinder, the <i>length</i> is the circumference of the circle,<br>ne <i>width</i> is the height of the can. |            |
| So: Surface Area | of a Cylinder = $2(area of a circle) + (circumference \cdot height)$  |            |
|                  | $\mathbf{SA} = 2\pi r^2 + 2\pi r \bullet h$   |            |

Volume: How much liquid could the soda can hold?

What do we know: Volume is the area of the base multiplied by the height.

So: Volume of a Cylinder = Area of Circle • Height of Can

$$\mathbf{V}=\pi r^2\bullet h$$

| Cylinder<br>Properties | Original | <b>4</b> x | 10x | 40x |
|------------------------|----------|------------|-----|-----|
| Diameter               |          |            |     |     |
| Radius                 |          |            |     |     |
| Height                 |          |            |     |     |
| Surface<br>Area        |          |            |     |     |
| Volume                 |          |            |     |     |

| Unit Activities:<br>Instructional<br>Events:         | Review, Understanding Bacterial<br>Growth, Bacterial Growth<br>Demonstration<br>Present the Stimulus, Provide<br>Learner Guidance   | Learning<br>Objectives:      | <ol> <li>Students will be able to:         <ol> <li>Recognize bacterial growth as an example of exponential growth, a non-linear function.</li> <li>Calculate the growth of bacteria over a given time period.</li> <li>Deconstruct and solve word problems.</li> <li>Describe the functional relationship between quantities in an exponential growth curve.</li> </ol> </li> </ol> |  |  |  |  |
|--|---|------------------------------|--|--|--|--|--|
| Materials:   | Modeling Clay   |                              |  |  |  |  |  |
| Student<br>Handouts:                                 | Understanding Bacterial Growth<br>handout (M27), Applying Bacterial<br>Growth Rates worksheet (pg. M30)   | Common<br>Core<br>Standards: | 8.F.1<br>8.F.4<br>8.F.5  |  |  |  |  |
| <b>Activities:</b><br>Review<br>(5 minutes)          | Daily Review Question: <b>Yesterday we learned about the size of bacteria. What surprised</b><br><b>you the most about what you learned yesterday? How big is a single bacterium cell? Is it</b><br><b>big or small?</b><br><b>Today we are going to continue talking about scale and the size of bacteria.</b>   |                              |  |  |  |  |  |
| Understanding<br>Bacterial<br>Growth<br>(15 minutes) | <ul> <li>Distribute a copy of <i>Understanding Bacterial Growth</i> to each student.</li> <li>Have students brainstorm ideas to compare and contrast bacterial growth with growth in animals and plants and record in the Venn diagram.</li> <li>Ask students to share ideas with the class.</li> <li>Ask students: If cells are so small, how do they grow fast enough to ever create an object you can see or one that could affect you?</li> <li>Take away point: ALL growth is a result of Cell Division</li> </ul> |                              |  |  |  |  |  |
|  | <ul> <li>double each time the cells regenerate</li> <li>Show students the following N<br/>http://www.youtube.com/wa</li> </ul>  | ouTube clip:                 | <u>dciWc</u>   |  |  |  |  |
|  | . U   |                              |  |  |  |  |  |
|  | • Explain that some bacteria, in often as every 20 minutes und  | -                            | hat make us sick like <i>E. coli,</i> can divide as<br>litions   |  |  |  |  |

Hands On: Real-World Lessons for Middle School Classrooms, University of Tennessee, 2018 This document may be reproduced and used for nonprofit, educational purposes without further permission so long as this copyright notice is included on all copies. Purpose: To facilitate the transfer of new knowledge to long-term retention by providing a concrete demonstration of an abstract concept.

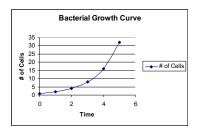
**Bacterial** Growth **Demonstration** (15minutes)

### Learner Level: All

- Give each student a golf-ball sized piece of clay that represents a single bacterium.
- Every 30 seconds, have each student divide his/her "bacteria": first two, then four, then eight, then 16, then 32 to demonstrate bacterial growth. (Total time: 2 min. 30 sec.)
  - Track bacterial growth on a class chart. Example:

| # of Divisions | Time Elapsed<br>in Seconds | # Cells |
|----------------|----------------------------|---------|
| 0              | 0                          | 1       |
| 1              | 30                         | 2       |
| 2              | 60                         | 4       |

- Ask students: What happens each time the cells divide? *the number of cells double*
- After students have finished dividing their "bacteria", show students how this activity represents a function, having an input and an output (x-axis: # of times cells divide, yaxis: # of bacteria cells). Plot the data points (ordered pairs) from the class chart onto a graph creating the exponential growth curve of bacterial growth, which is a non-linear function. Example:



Ask students to consider how their model bacteria are different from real life (size, structure, dividing bacteria do not get smaller and smaller with each generation and growth rates are not limitless).

Application of Purpose: To allow the learner to practice the new knowledge. The repetition further increases the likelihood of retention of the new information. (20 minutes)

- Give each student a copy of *Applying Bacterial Growth Rates* worksheet.
- Remind students that some bacteria, including strains that make us sick like *E. coli*, can divide as often as every 20 minutes under optimal conditions.
- Allow students time to answer the questions.
- **Discuss answers**

Tell students: Ask students:

Wrap Up (5 minutes)

Knowledge

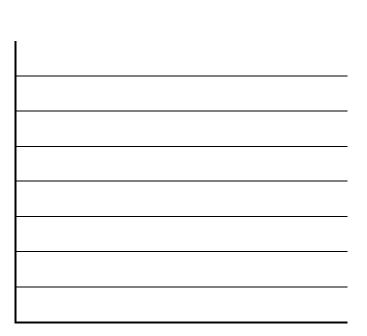
- How do bacteria grow?
  - Cell division, which causes the number of cells to increase rapidly
  - When charted, what kind of function does bacterial growth produce? 0 A non-linear function.

Tomorrow we will take what we know about bacterial growth and figure out if foods in different situations are safe for us to eat.

## **Applying Bacterial Growth Rates**

Use the chart below to track the growth of a single *E. coli* bacterium cell over several hours. Assume the cell has a generation time of 20 minutes. Then, create a graph of the exponential growth curve where the number of cell divisions are along the *x*-axis and the total number of bacterial cells are along the *y*-axis.

| # of<br>Divisions | Time Elapsed<br>in Minutes | # of Cells |
|-------------------|----------------------------|------------|
| 0                 | 0                          | 1          |
| 1                 | 20                         |            |
| 2                 | 40                         |            |
| 3                 | 60                         |            |
|                   |                            |            |
|                   |                            |            |
|                   |                            |            |
|                   |                            |            |
|                   |                            |            |
|                   |                            |            |



- 1. One *E. coli* cell could multiply up to \_\_\_\_\_ cells in just 1 hour.
- 2. How many *E. coli* cells would there be after 2 hours?
- 3. How many *E. coli* cells would there be after 3 hours?
- 4. If it takes 128 cells of *E. coli* to make you sick, and the cells can divide as often as every 20 minutes, then how long would it take for one cell to grow enough to make you sick?
- 5. Describe the relationship of the variables represented in the graph.

### **Tracking Bacterial Growth**:

*Shigella* (a type of bacteria) has a generation time of 40 minutes. Use the chart below to track the growth over several hours. Assume there are 4 cells present at start time. Then, create a graph of the exponential growth curve where the number of cell divisions are along the *x*-axis and the total number of bacterial cells are along the *y*-axis.

| # of<br>Divisions | Time Elapsed<br>in Minutes | # of Cells |
|-------------------|----------------------------|------------|
| 0                 | 0                          | 4          |
| 1                 | 40                         |            |
| 2                 | 80                         |            |
|                   |                            |            |
|                   |                            |            |
|                   |                            |            |
|                   |                            |            |
|                   |                            |            |
|                   |                            |            |

6. How many *Shigella* cells would there be after 2 hours?

7. How many *Shigella* cells would there be after 4 hours?

8. In optimal conditions, how many times would *Shigella* cells divide in 6 hours?

| Important information |        |  |  |  |  |
|-----------------------|--------|--|--|--|--|
| Total Time:           | 6 hrs  |  |  |  |  |
| Generation Time:      | 40 min |  |  |  |  |

**Step 1:** Convert the Total Time from hours to minutes

 $6 \text{ hrs} = \___ \text{min}$ 

**Step 2:** Divide Total Time by Generation Time

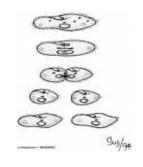
\_\_\_\_\_ min / \_\_\_\_\_ min = \_\_\_\_\_

9. In optimal conditions, how many times would Shigella cells divide in 8 hours?

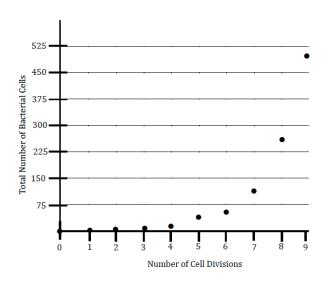
| Important information | <u>tion</u> |
|-----------------------|-------------|
| Total Time:           |             |
| Generation Time:      |             |

### **Applying Bacterial Growth Rates**

Use the chart below to track the growth of a single *E. coli* bacterium cell over several hours. Assume the cell has a generation time of 20 minutes. Then, create a graph of the exponential growth curve where the number of cell divisions are along the *x*-axis and the total number of bacterial cells are along the *y*-axis.



| # of<br>Divisions | Time Elapsed<br>in Minutes | # of Cells |
|-------------------|----------------------------|------------|
| 0                 | 0                          | 1          |
| 1                 | 20                         | 2          |
| 2                 | 40                         | 4          |
| 3                 | 60                         | 8          |
| 4                 | 80                         | 16         |
| 5                 | 100                        | 32         |
| 6                 | 120                        | 64         |
| 7                 | 140                        | 128        |
| 8                 | 160                        | 256        |
| 9                 | 180                        | 512        |



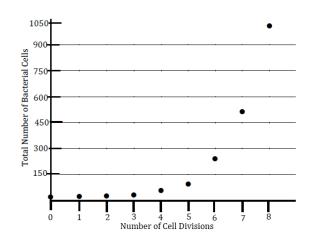
512

- 1. One *E. coli* cell could multiply up to <u>8</u> cells in just 1 hour.
- 2. How many *E. coli* cells would there be after 2 hours?64
- 3. How many *E. coli* cells would there be after 3 hours?
- 4. If it takes 128 cells of *E. coli* to make you sick, and the cells can divide as often as every 20 minutes, then how long would it take for one cell to grow enough to make you sick? 140 minutes
- 5. Describe the relationship of the variables represented in the graph.

### **Tracking Bacterial Growth**:

*Shigella* (a type of bacteria) has a generation time of 40 minutes. Use the chart below to track the growth over several hours. Assume there are 4 cells present at start time. Then, create a graph of the exponential growth curve where the number of cell divisions are along the *x*-axis and the total number of bacterial cells are along the *y*-axis.

| # of<br>Divisions | Time Elapsed<br>in Minutes | # of Cells |
|-------------------|----------------------------|------------|
| 0                 | 0                          | 4          |
| 1                 | 40                         | 8          |
| 2                 | 80                         | 16         |
| 3                 | 120                        | 32         |
| 4                 | 160                        | 64         |
| 5                 | 200                        | 128        |
| 6                 | 240                        | 256        |
| 7                 | 280                        | 512        |
| 8                 | 320                        | 1,024      |



32

256

- 6. How many *Shigella* cells would there be after 2 hours?
- 7. How many *Shigella* cells would there be after 4 hours?
- 8. In optimal conditions, how many times would Shigella cells divide in 6 hours?

| Important information |        |  |
|-----------------------|--------|--|
| Total Time:           | 6 hrs  |  |
| Generation Time:      | 40 min |  |

Step 1: Convert the Total Time from hours to minutes

6 hrs = 360 min

Step 2: Divide Total Time by Generation Time

<u>360</u> min / <u>40</u> min = <u>9</u>

9. In optimal conditions, how many times would Shigella cells divide in 8 hours?

| Important information |          |  |
|-----------------------|----------|--|
| l Time: <u>480 mi</u> | <u>n</u> |  |
| n Time: <u>40 mir</u> | <u>1</u> |  |

12 cell divisions

| Unit<br>Activities:<br>Instructional<br>Events: | Review, Application of Knowledge, Is<br>it Safe to Eat?<br>Elicit Performance, Provide<br>Feedback  | Learning<br>Objectives:   | <ol> <li>Students will be able to:         <ol> <li>Calculate the growth of bacteria over a given time period.</li> <li>Recognize bacterial growth as an example of a non-linear function.</li> <li>Generate ordered pairs of a non-linear function.</li> <li>Deconstruct and solve word problems involving exponential growth.</li> </ol> </li> </ol> |
|---|---|---------------------------|--|
| Materials:                                      | Calculators (optional)  |                           |  |
| Student<br>Handouts:                            | <i>Is it Safe To Eat?</i> worksheet (pg.<br>M38)  | Common Core<br>Standards: | 8.F.1<br>8.F.3   |
| <b>Activities:</b><br>Review<br>(5 minutes)     | Ask Students:<br>Yesterday we learned that bacterial growth occurs when the cells divide. How many<br>more cells are present after each division? (Twice the amount/Double)<br>Today we are going to solve some problems to determine if foods in different situations<br>are safe to eat.  |                           |  |
| Is it Safe to<br>Eat?<br>(15 minutes)           | <ul> <li>Purpose: To assess and facilitate further student learning.</li> <li>Learner Level: All <ul> <li>Give each student a copy of Is it Safe to Eat? worksheet.</li> <li>Work through the example with students and then let students complete Part 1.</li> <li>It is important to remind students that these are only examples and should not be used as a guide for whether food is safe.</li> <li>Remind students that in real life they would not know the number of pathogenic cells contaminating their food.</li> <li>Encourage students to share individual stories regarding food safety.</li> </ul> </li> </ul>   |                           |  |
| Exponential<br>Growth Curve<br>(35 minutes)     | <ul> <li>Tell students: We have been solving word problems about bacterial growth. Notice how we can plot our points from the table to create an exponential growth curve. Bacterial growth is one type of exponential growth.</li> <li>Remind students of the exponential growth curve you created as a class yesterday with the data from the table.</li> <li>Instruct students that just as a line has a standard equation: y = mx+b or Ax + By = C, the exponential growth curve (non-linear) also has an equation: y = a(1+b)<sup>x</sup>.</li> <li>Inform learners that the exponential growth curve equation can be used to solve the problems in another way besides in a chart or table.</li> <li>Solve the example problem from the <i>Is it Safe to Eat</i>? worksheet again this time using the exponential growth curve equation.</li> </ul> |                           |  |

Exponential Growth Curve (35 minutes) Display the parts of the equation for students and discuss:

| Variable Represents                             |             | For Bacterial Growth   |  |
|---|-------------|--|--|
| у   | Final count | Final # of cells   |  |
| a Original amount                               |             | # of cells present at start                                      |  |
| 1+bGrowth factor, where b is<br>the % of change |             | Bacterial growth is 100% (it doubles), so <i>b</i> is 100% or 1. |  |
| x Time  |             | # of times the cells divide                                      |  |

For the sample problem:

| Variable | Value                | Comments   |
|----------|----------------------|--|
| у ?      |                      | This is what we want to know                           |
| а        | 4                    | Problem tells us that 4 cells are present at start     |
| b        | <i>b</i> = 100% or 1 | b = 1, so $(1+b) = (1+1) = 2$                          |
| x 3      |                      | Total Time 2 hours (120 minutes) divided by Generation |
|          |                      | Time (40 minutes), then the cells will divide 3 times  |

Solving the equation:

$$y = a(1+b)^{x}$$
  
y = 4(1+1)<sup>3</sup>  
y = 4(2)<sup>3</sup>  
y = 4(8)  
y = 32

Ask students: Is this the same answer we got the first time we solved this and worked it using the table? If it takes 10 cells to make you sick, is it safe to eat?

Tell students: **Right now you may not see how this would be a good tool, but what if I asked you how many cells would be present after 8 hours? How many of you have ever left food out overnight? That would take a long time to solve using the table.** 

| Important Information |                 | FORMULA:                |   | $y = a(1+b)^x$ |
|-----------------------|-----------------|-------------------------|---|----------------|
| Total Time:           | 8 hrs = 480 min | # of cells at start     | а | 4 cells        |
| Generation Time:      | 40 min          | Growth Rate             | b | 100% or 1      |
| Infectious dose:      |                 | # of times cells divide | x | (480/40) = 12  |

 $y = 4(1 + 1)^{12}$   $y = 4(2)^{12}$  y = 4(4096)y = 16,384

- Graph the curve using data from both the table and the equation results.
- Now have students complete **Part 2** of the *Is it Safe to Eat?* worksheet where they will practice solving for the exponential growth curve.

Tell students: Today we learned how to solve word problems to determine if food is safe to eat in specific situations. We used both tables and formulas to solve problems and realized they both lead you to the same answer. Tomorrow we will analyze the results of your bacterial growth labs from Science.

Wrap Up (5 minutes)

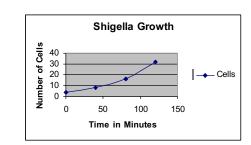
# Is it Safe to Eat?

# <u>PART 1 Directions:</u> For each of the scenarios using the information provided, complete the table and determine if the food is safe to eat.

**Example:** *Shigella* has a generation time of 40 minutes and an infectious dose of 10 cells. Mom's tuna salad was infected with 4 cells of *Shigella* and has been sitting on the dining room table for 2 hours. Is it safe to eat?

| Important Information       | Bacteria type: Shigella      |
|-----------------------------|------------------------------|
| Total Time: 2 hours         | Infectious dose: 10 cells    |
| Generation time: 40 minutes | # of cells at start: 4 cells |

| # of Times<br>Cells Divide | Time Elapsed in<br>Minutes | Number of<br>Cells |
|----------------------------|----------------------------|--------------------|
| 0                          | 0                          | 4                  |
| 1                          | 40                         | 8                  |
| 2                          | 80                         | 16                 |
| 3                          | 120                        | 32                 |



### No, the tuna salad is not safe to eat after 2 hours of sitting on the table.

1. *E. coli* O157:H7 has a generation time of 20 minutes and can make you sick with as few as 10 cells. Judy likes to eat her hamburgers medium rare. If her hamburger was contaminated with 2 *E. coli* O157:H7 cells that were not killed during cooking and she waited 20 minutes to eat the hamburger, is it safe to eat?

| Important Information | Bacteria type:       |  |
|-----------------------|----------------------|--|
| Total Time:           | Infectious dose:     |  |
| Generation Time:      | # of cells at start: |  |

| # of Times<br>Cells Divide | Time Elapsed<br>in Minutes | Number of<br>Cells |
|----------------------------|----------------------------|--------------------|
|                            |                            |                    |
|                            |                            |                    |
|                            |                            |                    |
|                            |                            |                    |

Is it safe to eat?

Hands On: Real-World Lessons for Middle School Classrooms,© University of Tennessee, 2018 This document may be reproduced and used for nonprofit, educational purposes without further permission so long as this copyright notice is included on all copies. 2. Under ideal conditions, *Salmonella* has a generation time of 30 minutes and an infectious dose of 15-20 cells. Aunt Susie's homemade Ranch salad dressing has been sitting on the picnic table for 2.5 hours. If the dressing started out infected with 3 *Salmonella* cells, is it safe to eat now?

| Important Information |  | Bacteria type:       |  |
|-----------------------|--|----------------------|--|
| Total Time:           |  | Infectious dose:     |  |
| Generation Time:      |  | # of cells at start: |  |

| # of Times<br>Cells Divide | Time Elapsed<br>in Minutes | Number of<br>Cells |
|----------------------------|----------------------------|--------------------|
|                            |                            |                    |
|                            |                            |                    |
|                            |                            |                    |
|                            |                            |                    |
|                            |                            |                    |
|                            |                            |                    |

\_\_\_\_\_

Is it safe to eat?

3. Using the information provided, write your own food safety scenario. Then, complete the table and to determine if the food is safe to eat.

| Important Information |            | Bacteria type:       | Campylobacter jejuni |
|-----------------------|------------|----------------------|----------------------|
| Total Time:           | 3 hours    | Infectious dose: _   | 400-500 cells        |
| Generation Time:      | 90 minutes | # of cells at start: | 150 cells            |

#### Scenario:

| # of Times<br>Cells Divide | Time Elapsed<br>in Minutes | Number of<br>Cells |
|----------------------------|----------------------------|--------------------|
|                            |                            |                    |
|                            |                            |                    |
|                            |                            |                    |
|                            |                            |                    |

Is it safe to eat? \_\_\_\_\_

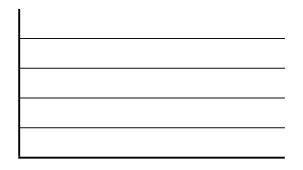
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# <u>PART 2 Directions:</u> Now, rather than using a table, use the formula for exponential growth to determine if the food is safe to eat. Show your work. Then create a line graph for each scenario illustrating the exponential growth curve.

4. *E. coli O157:H7* has a generation time of 20 minutes and can make you sick with as few as 10 cells. If Judy's hamburger was contaminated with 2 *E. coli* O157:H7 cells that were not killed during cooking, determine if it is safe to eat in each of the following situations.

| Important Information | FORMULA:                     | $y=a(1+b)^x$ |
|-----------------------|------------------------------|--------------|
| Total Time:           | # of cells at start: $a$     | 2 cells      |
| Generation Time:      | Growth Rate: b               | 100% or 1    |
| Infectious dose:      | # of times cells divide: $x$ |              |

- a. How many *E. coli* cells would be present (*y*) if she waited 40 minutes to eat the hamburger? Is it safe to eat?
- b. How many *E. coli* cells would be present (*y*) if she waited 1 hour to eat the hamburger? Is it safe to eat?
- c. Create a graph of the exponential growth curve where the number of times the cells divide is along the *x*-axis and the total number of bacterial cells is along the *y*-axis.



**CHALLENGE**: How many *E. coli* cells would be present (*y*) if she waited 3 hours to eat the hamburger?

5. Under ideal conditions, *Salmonella* has a generation time of 30 minutes and an infectious dose of 15-20 cells. If the dressing started out infected with 3 *Salmonella* cells, determine if it is safe to eat in each of the following situations.

| Important Information | FORMULA: $y=a(1+b)^x$      |
|-----------------------|----------------------------|
| Total Time:           | # of cells at start: a     |
| Generation Time:      | Growth Rate: <i>b</i>      |
| Infectious dose:      | # of times cells divide: x |

- a. How many *Salmonella* cells would be present (*y*) if the homemade salad dressing had been sitting on the picnic table for 1 hour? Is it safe to eat?
- b. How many *Salmonella* cells would be present (*y*) if the homemade salad dressing had been sitting on the picnic table for 3 hours? Is it safe to eat?

c. Create a graph of the exponential growth curve where the number of times the cells divide is along the *x*-axis and the total number of bacterial cells is along the *y*-axis.

**CHALLENGE**: How many *Salmonella* cells would be present (*y*) if the homemade salad dressing had been sitting on the picnic table for 6.5 hours?

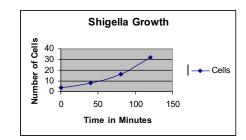


## <u>PART 1 Directions:</u> For each of the scenarios using the information provided, complete the table and determine if the food is safe to eat.

**Example:** *Shigella* has a generation time of 40 minutes and an infectious dose of 10 cells. Mom's tuna salad was infected with 4 cells of *Shigella* and has been sitting on the dining room table for 2 hours. Is it safe to eat?

| Important Information |        | Bacteria type:       | Shigella |
|-----------------------|--------|----------------------|----------|
| Total Time:           | 2 hrs  | Infectious dose:     | 10 cells |
| Generation Time:      | 40 min | # of cells at start: | 4 cells  |

| # of Times<br>Cells Divide | Time Elapsed in<br>Minutes | Number of<br>Cells |
|----------------------------|----------------------------|--------------------|
| 0                          | 0                          | 4                  |
| 1                          | 40                         | 8                  |
| 2                          | 80                         | 16                 |
| 3                          | 120                        | 32                 |



No, the tuna salad is not safe to eat after 2 hours of sitting on the table.

1. *E. coli O157:H7* has a generation time of 20 minutes and can make you sick with as few as 10 cells. Judy likes to eat her hamburgers medium rare. If her hamburger was contaminated with 2 *E. coli O157:H7* cells that were not killed during cooking and she waited 20 minutes to eat the hamburger, is it safe to eat?

| Important Info   | ormation   | Bacteria type:       | <i>E. coli</i> O157:H7 |
|------------------|------------|----------------------|------------------------|
| Total Time:      | 20 minutes | Infectious dose:     | 10 cells               |
| Generation Time: | 20 minutes | # of cells at start: | 2 cells                |

| # of Times<br>Cells Divide | Time Elapsed<br>in Minutes | Number of<br>Cells |
|----------------------------|----------------------------|--------------------|
| 0                          | 0                          | 2                  |
| 1                          | 20                         | 4                  |
|                            |                            |                    |
|                            |                            |                    |

## Is it safe to eat? Yes, it is safe.

2. Under ideal conditions, *Salmonella* has a generation time of 30 minutes and an infectious dose of 15-20 cells. Aunt Susie's homemade Ranch salad dressing has been sitting on the picnic table for 2.5 hours. If the dressing started out infected with 3 *Salmonella* cells, is it safe to eat now?

| Important Information |            | Bacteria type:       | Salmonella     |
|-----------------------|------------|----------------------|----------------|
| Total Time:           | 2.5 hours  | Infectious dose:     | 15-20 cells    |
| Generation Time:      | 30 minutes | # of cells at start: | <u>3 cells</u> |

| # of Times<br>Cells Divide | Time Elapsed<br>in Minutes | Number of<br>Cells |
|----------------------------|----------------------------|--------------------|
| 0                          | 0                          | 3                  |
| 1                          | 30                         | 6                  |
| 2                          | 60                         | 12                 |
| 3                          | 90                         | 24                 |
| 4                          | 120                        | 48                 |
| 5                          | 150                        | 96                 |

## Is it safe to eat? No, it is not safe

3. Using the information provided, write your own food safety scenario. Then, complete the table and to determine if the food is safe to eat.

| Important Information |            | Bacteria type:       | Campylobacter jejuni |
|-----------------------|------------|----------------------|----------------------|
| Total Time:           | 3 hours    | Infectious dose:     | 400-500 cells        |
| Generation Time:      | 90 minutes | # of cells at start: | 150 cells            |

#### Scenario:

| # of Times<br>Cells Divide | Time Elapsed<br>in Minutes | Number of<br>Cells |
|----------------------------|----------------------------|--------------------|
| 0                          | 0                          | 150                |
| 1                          | 90                         | 300                |
| 2                          | 180                        | 600                |

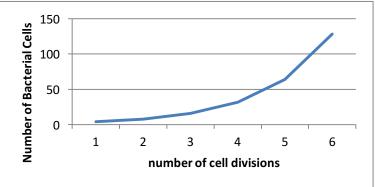
Is it safe to eat? No, it is not safe

# <u>PART 2 Directions:</u> Now, rather than using a table, use the formula for exponential growth to determine if the food is safe to eat. Show your work. Then create a line graph for each scenario illustrating the exponential growth curve.

4. *E. coli O157:H7* has a generation time of 20 minutes and can make you sick with as few as 10 cells. If Judy's hamburger was contaminated with 2 *E. coli O157:H7* cells that were not killed during cooking, determine if it is safe to eat in each of the following situations.

| Important Information | FORMULA:                                 | $y=a(1+b)^x$ |
|-----------------------|--|--------------|
| Total Time:           | # of cells at start: $a$                 | 2 cells      |
| Generation Time:      | Growth Rate: b                           | 100% or 1    |
| Infectious dose:      | $\frac{1}{2}$ # of times cells divide: x |              |

- a. How many *E. coli* cells would be present (*y*) if she waited 40 minutes to eat the hamburger? Is it safe to eat?
- Solution: If the total time is 40 minutes, then the cells divide 2 times, so $y = 2(1 + 1)^2 = 8$  cells. This is less than the infectious dose of 10 cells. Yes, it is safe to eat.
  - b. How many *E. coli* cells would be present (*y*) if she waited 1 hour to eat the hamburger? Is it safe to eat?
- Solution: If the total time is 60 minutes, the cells divide 3 times, so  $y = 2(1 + 1)^3 = 16$  cells. This is more than the infectious dose of 10 cells. No, it is not safe to eat.
  - c. Create a graph of the exponential growth curve where the number of times the cells divide is along the *x*-axis and the total number of bacterial cells is along the *y*-axis.



**CHALLENGE**: How many *E. coli* cells would be present (*y*) if she waited 3 hours to eat the hamburger?

$$y = 2(1+1)^9 = 1024$$
 cells

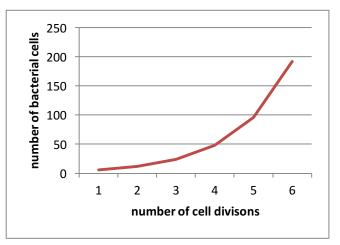
5. Under ideal conditions, *Salmonella* has a generation time of 30 minutes and an infectious dose of 15-20 cells. If the dressing started out infected with 3 *Salmonella* cells, determine if it is safe to eat in each of the following situations.

| Important Information | FORMULA: $y=a(1+b)^x$         |
|-----------------------|-------------------------------|
| Total Time:           | # of cells at start: <i>a</i> |
| Generation Time:      | Growth Rate: <i>b</i>         |
| Infectious dose:      | # of times cells divide: x    |

- a. How many *Salmonella* cells would be present (*y*) if the homemade salad dressing had been sitting on the picnic table for 1 hour? Is it safe to eat?
- Solution: If the total time is 60 minutes, then the cells divide 2 times, so  $y = 3(1 + 1)^2 = 12$  cells. This is less than the infectious dose of 15-20 cells. Yes, it is safe to eat.
  - b. How many *Salmonella* cells would be present (*y*) if the homemade salad dressing had been sitting on the picnic table for 3 hours? Is it safe to eat?

Solution: If the total time is 90 minutes, then the cells divide 3 times, so  $y = 3(1 + 1)^6 = 192$  cells. This is more than the infectious dose of 15-20 cells. No, it is not safe to eat.

c. Create a graph of the exponential growth curve where the number of times the cells divide is along the *x*-axis and the total number of bacterial cells is along the *y*-axis.



**CHALLENGE**: How many *Salmonella* cells would be present (*y*) if the homemade salad dressing had been sitting on the picnic table for 6.5 hours?

| Unit<br>Activities:<br>Instructional<br>Events:<br>Materials: | Review, Student Reflection, Analyzing<br>Data<br>Assessing Performance, Enhance<br>Retention & Transfer<br>Construction paper  | Learning<br>Objectives:   | <ol> <li>Students will be able to:         <ol> <li>Use mean, median, mode, and range to analyze a data set.</li> <li>Use statistical analysis to compare treatments in a data set.</li> <li>Create graphical representations of data.</li> <li>Interpret graphical representations of data sets.</li> </ol> </li> </ol> |  |  |  |
|---|--|---------------------------|--|--|--|--|
| Student<br>Handouts:  | Analyzing Data worksheet (pg. M45)<br>Analyzing Data Self-Assessment (pg.<br>M47)  | Common Core<br>Standards: | 8.SP.1<br>8.SP.2   |  |  |  |
| <b>Activities:</b><br>Review<br>(5 minutes)                   | Daily Review Question: <b>Yesterday we solved some problems to determine if foods in different</b><br>situations are safe to eat. Today we are going to analyze the results of your bacterial growth<br>labs from science class. What predictions do you have as to which treatment was the most<br>effective in getting rid of bacteria?  |                           |  |  |  |  |
| Student<br>Reflection<br>(15 minutes)                         | <ul> <li>Purpose: To determine if students are successfully meeting the learning objectives for this lesson</li> <li>Learner Level: All <ul> <li>Ask students to reflect on the math concepts they have learned so far (bacterial growth and scale).</li> <li>Allow students to work in pairs and provide each pair with a piece of construction paper.</li> <li>Each pair should write one "really good" multiple-choice test question that covers the math concepts they've learned so far in this lesson.</li> <li>Post each pairs question on the front board and, as a class, try to answer each question correctly.</li> </ul> </li> </ul> |                           |  |  |  |  |
| Analyzing<br>Bacterial<br>Growth Data<br>(30 minutes)         | <ul> <li>Purpose: To allow students to develop expertise with the new information and create a construct for transferring knowledge to long-term retention.</li> <li>Learner Level: All <ul> <li>Using the raw data collected in the science follow-up lab, have students complete the Analyzing Data worksheet.</li> <li>Students may work individually or in pairs.</li> <li>Once they have finished, have students complete the Analyzing Data Self-Assessment.</li> <li>Modifications for lower level students include: completing the exercise as a group and reducing the number of problems.</li> </ul> </li> </ul>                       |                           |  |  |  |  |

Wrap Up (5 minutes) Ask students: Were your predictions correct? What treatment was the most effective?



• List all the data points collected for the **unwashed hands treatment** from your Bacterial Growth Experiment in Science in order from least to greatest.



- List all the data points from the hands **washed with cold water for 5 seconds treatment** in order from least to greatest.
- List all the data points from the hands washed with warm water and soap for 20 seconds treatment in order from least to greatest.
- List all the data points from the hands with sanitizer treatment in order from least to greatest.
- Using data set for the **unwashed hands treatment** construct a frequency table. Be sure to choose regular intervals. Use the frequency table to create a histogram.

- What trends do you notice when you examine the histogram?
- Use the **washed with cold water for 5 seconds treatment** data set to construct a box and whiskers plot:
  - a. Identify the upper and lower extremes. Upper: Lower:
  - b. Identify the median. Median:
  - c. Find the  $1^{st}$  and  $3^{rd}$  quartiles.  $1^{st}$  quartile:  $3^{rd}$  quartile:
  - d. Draw the plot below.



### Analyzing Data Page 2

- Use the **washed with warm water and soap for 20 seconds treatment** data set to construct a box and whiskers plot:
  - a. Identify the upper and lower extremes. Upper: Lower:
    b. Identify the median. Median:
    c. Find the 1<sup>st</sup> and 3<sup>rd</sup> quartiles. 1<sup>st</sup> quartile: 3<sup>rd</sup> quartile:
    d. Draw the plot below.
- Answer the following questions using the two box and whiskers plots you constructed.
  - a. Which treatment had the highest median colony growth?

b. Is there a difference in the colony growth resulting from the two different treatments? For example, are the medians different? Are the middle 50%'s different? If so, explain why you think this difference exists.

- c. Which treatment had the smallest range? Why do you think this is?
- For each treatment, find the mean, median, mode, and range. Record your answers in the chart below:

| Treatment                    | Mean | Median | Mode | Range |
|------------------------------|------|--------|------|-------|
| Unwashed hands               |      |        |      |       |
| Cold water for 5 sec         |      |        |      |       |
| Warm water & soap for 20 sec |      |        |      |       |
| Sanitizer                    |      |        |      |       |

- Use the means for each of the four treatments to construct a scatter plot below:
  - Based on the scatter plot you constructed would you say there is a positive relationship, negative relationship, or no relationship between the hand washing treatments and the number of bacterial colonies?